

2.1

Given that  $P(A) = 2/3$ ,  $P(B) = 1/6$ ,  $P(A \cap B) = 1/9$ , what is  $P(A \cup B)$ ?

We know that  $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ .

So  $P(A \cup B) = 2/3 + 1/6 - 1/9 = 9/18 + 3/18 - 2/18 = 10/18 = 5/9$

2.2

The probability that at least one of E or F occurs,  $P(E \cup F) = 3/4$ . We wish to find

We wish to find the probability that neither E nor F occurs, i.e.  $P(E' \cap F')$ .

By deMorgan's Law,  $E' \cap F' = (E \cup F)' = 1 - P(E \cup F) = 1 - 3/4 = 1/4$ .

2.4

The probability that of A, B, and C, A alone occurs =  $P(A \cap (B' \cap C'))$

=  $P((A' \cup B \cup C)')$  deMorgan's law

=  $1 - P(A' \cup (B \cup C))$  (since  $P(E') = 1 - P(E)$ )

=  $1 - [P(A') + P(B \cup C) - P(A' \cap (B \cup C))]$  probability of an "or"

(\*) =  $P(A) + P(A' \cap (B \cup C)) - P(B \cup C)$  (replacing  $P(A')$  with  $1 - P(A)$  and rearranging

Now, A and A' are clearly disjoint, and therefore A and A'  $\cap$  (B  $\cup$  C) must also be

disjoint. Furthermore, A  $\cup$  A' is the entire sample space, so we can write

$P(A \cup B \cup C) = P((A \cup A') \cap (A \cup B \cup C)) = P(A \cup [A' \cap (B \cup C)])$

=  $P(A) + P(A' \cap (B \cup C))$ .

Substituting this into (\*), we get

$P(A \cap B' \cap C') = P(A \cup B \cup C) - P(B \cup C)$ . Finally, since

$P(B \cup C) = P(B) + P(C) - P(B \cap C)$ , we end up with

$P(A \cap B' \cap C') = P(A \cup B \cup C) - P(B) - P(C) + P(B \cap C)$

2.9

A: throw tails exactly 2 times: HTT THT TTH

B: throw tails at least 2 times: HTT THT TTH TTT

C: tails did not appear before a head appeared: HHH HTH HHT HTT

D: first result is a tail: THH THT TTH TTT

2.13:

Could get:

a,b a,c a,d

b,a b,c b,d

c,a c,b c,d

d,a d,b d,c

	a	b	c	d
a	0	1/12	1/12	1/12
b	1/12	0	1/12	1/12
c	1/12	1/12	0	1/12
d	1/12	1/12	1/12	0

